

1 (c) Since $n = 9 \neq 1$, the algorithm sets $m = \lfloor \frac{9}{2} \rfloor = 4$. Since $x = 10 > a_4 = 4$, the algorithm replaces n by $n - m = 5$ and changes the list to 5, 6, 7, 8, 9.

Since $n \neq 1$, the algorithm sets $m = \lfloor \frac{5}{2} \rfloor = 2$. Since $x = 10 > a_2 = 6$, the algorithm replaces n with $n - m = 3$ and changes the list to 7, 8, 9.

Since $n \neq 1$, the algorithm sets $m = \lfloor \frac{3}{2} \rfloor = 1$. Since $x = 10 > a_1 = 7$, the algorithm replaces n with $n - m = 2$ and changes the list to 8, 9.

Since $n \neq 1$, the algorithm sets $m = \lfloor \frac{2}{2} \rfloor = 1$. Since $x = 10 > a_1 = 8$, the algorithm replaces n with $n - m = 1$ and changes the list to 9.

Since $n = 1$ and $x = 10 \neq a_1 = 9$, the algorithm outputs "false," sets $n = 0$ and stops.

This search required five comparisons of x with other elements; a linear search would have required nine.

8.	\mathcal{L}_1	\mathcal{L}_2	\mathcal{L}_3
	2, 4, 4, 6, 8	1, 5, 7, 9, 10	
	2, 4, 4, 6, 8	5, 7, 9, 10	1
	4, 4, 6, 8	5, 7, 9, 10	1, 2
	4, 6, 8	5, 7, 9, 10	1, 2, 4
	6, 8	5, 7, 9, 10	1, 2, 4, 4
	6, 8	7, 9, 10	1, 2, 4, 4, 5
	8	7, 9, 10	1, 2, 4, 4, 5, 6
	8	9, 10	1, 2, 4, 4, 5, 6, 7
			1, 2, 4, 4, 5, 6, 7, 8, 9, 10

The algorithm required seven comparisons.

14. (a) Here's the bubble sort:

$k = 6:$ \rightarrow <u>7</u> , 2, 2, 5, 3, 5, 4 \rightarrow 2, <u>7</u> , 2, 5, 3, 5, 4 \rightarrow 2, 2, <u>7</u> , 5, 3, 5, 4 \rightarrow 2, 2, 5, <u>7</u> , 3, 5, 4 \rightarrow 2, 2, 5, 3, <u>7</u> , 5, 4 \rightarrow 2, 2, 5, 3, 5, <u>7</u> , 4	$k = 5:$ \rightarrow <u>2</u> , 2, 5, 3, 5, 4, 7 \rightarrow 2, <u>2</u> , 5, 3, 5, 4, 7 \rightarrow 2, 2, <u>5</u> , 3, 5, 4, 7 \rightarrow 2, 2, 3, <u>5</u> , 5, 4, 7 \rightarrow 2, 2, 3, 5, <u>5</u> , 4, 7
$k = 4:$ \rightarrow <u>2</u> , 2, 3, 5, 4, 5, 7 \rightarrow 2, <u>2</u> , 3, 5, 4, 5, 7 \rightarrow 2, 2, <u>3</u> , 5, 4, 5, 7 \rightarrow 2, 2, 3, <u>5</u> , 4, 5, 7	$k = 3:$ \rightarrow <u>2</u> , 2, 3, 4, 5, 5, 7 \rightarrow 2, <u>2</u> , 3, 4, 5, 5, 7 \rightarrow 2, 2, <u>3</u> , 4, 5, 5, 7
$k = 2:$ \rightarrow <u>2</u> , 2, 3, 4, 5, 5, 7 \rightarrow 2, <u>2</u> , 3, 4, 5, 5, 7	$k = 1:$ \rightarrow <u>2</u> , 2, 3, 4, 5, 5, 7 \rightarrow 2, <u>2</u> , 3, 4, 5, 5, 7

This required a total of $6 + 5 + 4 + 3 + 2 + 1 = \frac{(6)(7)}{2} = 21$ comparisons.

(b) Here's the merge sort.

Step 2: 7; 2; 2; 5; 3; 5; 4;

Step 3: 2, 7; 2, 5; 3, 5; 4

Step 3: 2, 2, 5, 7; 3, 4, 5

Step 3: 2, 2, 3, 4, 5, 5, 7

Merging two lists of length 1 to one of length 2 requires $1 + 1 - 1 = 1$ comparison. Thus, the initial merging of seven lists of length 1 to three of length 2 and one of length 1 required $1 + 1 + 1 = 3$ comparisons. The merging of three lists of length 2 and one of length 1 to one list of length 4 and another of length 3 required $(2 + 2 - 1) + (2 + 1 - 1) = 5$ comparisons. The final merging required $4 + 3 - 1 = 6$ comparisons. The total is $3 + 5 + 6 = 14$ comparisons.